

Coimisiún na Scrúduithe Stáit State Examinations Commission

Junior Certificate 2018

Marking Scheme

Mathematics

Higher Level

Note to teachers and students on the use of published marking schemes

Marking schemes published by the State Examinations Commission are not intended to be standalone documents. They are an essential resource for examiners who receive training in the correct interpretation and application of the scheme. This training involves, among other things, marking samples of student work and discussing the marks awarded, so as to clarify the correct application of the scheme. The work of examiners is subsequently monitored by Advising Examiners to ensure consistent and accurate application of the marking scheme. This process is overseen by the Chief Examiner, usually assisted by a Chief Advising Examiner. The Chief Examiner is the final authority regarding whether or not the marking scheme has been correctly applied to any piece of candidate work.

Marking schemes are working documents. While a draft marking scheme is prepared in advance of the examination, the scheme is not finalised until examiners have applied it to candidates' work and the feedback from all examiners has been collated and considered in light of the full range of responses of candidates, the overall level of difficulty of the examination and the need to maintain consistency in standards from year to year. This published document contains the finalised scheme, as it was applied to all candidates' work.

In the case of marking schemes that include model solutions or answers, it should be noted that these are not intended to be exhaustive. Variations and alternatives may also be acceptable. Examiners must consider all answers on their merits, and will have consulted with their Advising Examiners when in doubt.

Future Marking Schemes

Assumptions about future marking schemes on the basis of past schemes should be avoided. While the underlying assessment principles remain the same, the details of the marking of a particular type of question may change in the context of the contribution of that question to the overall examination in a given year. The Chief Examiner in any given year has the responsibility to determine how best to ensure the fair and accurate assessment of candidates' work and to ensure consistency in the standard of the assessment from year to year. Accordingly, aspects of the structure, detail and application of the marking scheme for a particular examination are subject to change from one year to the next without notice.

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Paper 1

Structure of the marking scheme

Candidate responses are marked according to different scales, depending on the types of response anticipated. Scales labelled A divide candidate responses into two categories (correct and incorrect), scales labelled B divide responses into three categories (correct, partially correct, and incorrect), and so on. The scales and the marks that they generate on this examination paper are summarised in this table:

Scale label	Scale label B		D
No of categories	3	4	5
5-mark scale	0, 3, 5	0, 2, 3, 5	0, 2, 3, 4, 5
10-mark scale		0, 3, 7, 10	0, 2, 6, 9, 10
15-mark scale		0, 4, 12, 15	0, 3, 9, 13, 15

A general descriptor of each point on each scale is given below. More specific directions in relation to interpreting the scales in the context of each question are given in the scheme, where necessary.

Marking scales – level descriptors

B-scales (three categories)

- response of no substantial merit (no credit)
- partially correct response (partial credit)
- correct response (full credit)

C-scales (four categories)

- response of no substantial merit (no credit)
- response with some merit (low partial credit)
- almost correct response (high partial credit)
- correct response (full credit)

D-scales (five categories)

- response of no substantial merit (no credit)
- response with some merit (low partial credit)
- response about half-right (mid partial credit)
- almost correct response (high partial credit)
- correct response (full credit)

In certain cases, typically involving incorrect rounding, omission of units, a misreading that does not oversimplify the work, or an arithmetical error that does not oversimplify the work, a mark that is one mark below the full-credit mark may be awarded. This level of credit is referred to as *Full Credit* -1, and these types of errors are identified with an asterisk (*). Thus, for example, in Scale 10C, *Full Credit* -1 of 9 marks may be awarded.

No marks may be awarded other than those on the appropriate scale, and *Full Credit* -1.

Question	1 (20)	Question 6	6 (40)	Question 2	10 (30)
(a)	5B	(a) <i>,</i> (b)	10C	(a)	15C
(b)	15C	(c) <i>,</i> (d)	10D	(b)	10C
		(e) <i>,</i> (f)	10D	(c)	5B
Question	2 (30)	(g) <i>,</i> (h)	10C		
(a)	10C			Question 2	11 (10)
(b)	10D	Question 7	7 (15)		10D
(c)	10D	(a)	5C		
		(b)	10C	Question 2	12 (15)
Question	3 (10)			(a)	10D
(a) <i>,</i> (b)	10D	Question 8	8 (25)	(b)	5C
		(a)	15C		
Question	4 (15)	(b)	10C	Question 2	13 (15)
(a)	5C			(a) <i>,</i> (b)	15D
(b)	10C	Question 9	9 (25)		
		(a)	5B	Question 2	14 (25)
Question	5 (25)	(b),(c)	5D	(a)	15C
(a)	5B	(d)	5B	(b)	10C
(b)	10D	(e)	10D		
(c)	10C				

Summary of mark allocations and scales to be applied

Model Solutions & Marking Notes

The model solutions for each question are not intended to be exhaustive – there may be other correct solutions. Any Examiner unsure of the validity of the approach adopted by a particular candidate to a particular question should contact his / her Advising Examiner.

Where the scheme refers to "work of merit", examples are given of the standard acceptable as work of merit in that particular part.

In general, accept a candidate's work in one part of a question for use in subsequent parts of the question, unless this oversimplifies the work involved.

Q1	Model Solution – 20 Marks	Marking Notes
(a)	1st Difference = $7 - 1 = 6$	Scale 5B (0, 3, 5)
	Answer: 13, 19, 25	Accept correct answer without supporting work.
		Partial Credit
		 Shows understanding of linear patterns, for example: explains linear properly; correct first difference found
		 Three consecutive terms in linear sequence (possibly including 1 and 7)
		• Correct relevant formula, for example: $T_n = a + (n - 1)d$ or $y = mx + c$
		Full Credit –1
		 Apply a * if two of the new first differences are 6, for example: 13, 19, 26 or 12, 18, 24.
(b)	(b) Any pattern continuing on from 1, 7	Scale 15C (0, 4, 12, 15)
	with a (non-zero) constant second difference.	Accept correct answer without supporting work.
	For example: 14, 22, 31	• Answer of 13, 19, 25, or finds first difference
	or any other quadratic sequence continuing on from 1, 7	 Low Partial Credit Shows understanding of quadratic patterns, for example: indicates or refers to second differences Correct relevant formula, for example: an² + bn + c
		 High Partial Credit Writes sequence with at least 2 equal non-zero second differences (not necessarily consecutive)

Q2	Model Solution – 30 Marks				Marking Notes
(a)	(i) 750 [kcal]				Scale 10C (0, 3, 7, 10)
					Accept correct answer without supporting
	(ii) 3	00 kcal in 3	30 mins		Tolerance: ± 10 on y-axis and ± 1 on y-axis
	n n	1 F F [boot	kcal in 1 ho	our tol	Low Partial Credit.
	∴ 155 [beats per minute]			lej	 Work of merit in (i) or (ii), for example: relevant indication on graph for either part (including indication of 300 kcal); or 125 given as answer in (ii)
					High Partial Credit
					• (i) or (ii) correct
					Work of merit in both parts
(b)	Stage	Slow	Sprint	Total	Scale 10D (0, 2, 6, 9, 10)
	1	60	50	110	Accept correct answer without supporting
	2	60	100	160	Work
	3	60	150	210	Note: Accept Total as correct if it is either
	4	60	200	260	or (for stages 3, 4, and 5) if it is 50 greater
	5	60	250	310	than the Total from the previous row.
	n	60	50n	60 + 50n	<i>Note</i> : If final Sprint entry not in terms of <i>n</i> , award <i>MPC</i> at most.
					Low Partial Credit
					One entry correct
					Mid Partial CreditFive entries correct
					 <i>High Partial Credit</i> Seven entries correct, including at least one of the entries in terms of n
					 Full Credit –1 Nine entries correct (i.e. all but one), including both of the entries in terms of n

Q2	Model Solution – 30 Marks	Marking Notes
(c)	Total distance $= 60 + 150 = 210$ [m]	Scale 10D (0, 2, 6, 9, 10)
	Slow run: Time = $\frac{D}{s} = \frac{60}{2} = 30$ [seconds] Sprint: Time = $\frac{D}{s} = \frac{150}{7\cdot 5} = 20$ [seconds] Total time = $30 + 20 = 50$ [seconds]	 Low Partial Credit Work of merit, for example: relevant formula; finds total distance Mid Partial Credit One correct time calculated
	Average Speed $=\frac{D}{T} = \frac{210}{50} = 4 \cdot 2 \text{ [m/s]}$	 High Partial Credit Total stage time calculated One correct time calculated and 210 divided by some incorrect figure derived from some work of merit Correct answer with no supporting work

Q3	Model Solution – 10 Marks	Marking Notes
(a) <i>,</i> (b)	(a) $\frac{14}{35} \times 100 = \frac{2}{5} \times 100 = 40$ [%] (b) $\frac{200}{0.88} = €227 \cdot 27$	 Scale 10D (0, 2, 6, 9, 10) Accept correct answer without supporting work Low Partial Credit Work of merit in (a) or (b), that is: a relevant product or relevant quotient (including reciprocals)
	$227 \cdot 27 \dots \times 1 \cdot 18 = 268 \cdot 181 \dots$ $= [\$] 268 \cdot 18 [2 \text{ D.P.}]$ OR $\frac{1 \cdot 18}{0 \cdot 88} = 1 \cdot 3409 \dots$	 Mid Partial Credit (a) correct Work of merit in (a) and (b) High Partial Credit (a) correct, and work of merit in (b) (b) correct
	So $\pounds 1 = \$1 \cdot 3409$ $\pounds 200 \times 1 \cdot 3409 = 268 \cdot 18$ $= [\$] 268 \cdot 18 [2 D.P.]$ OR	 Full Credit –1 Incorrect or no rounding
	$\frac{0.88}{1.18} = 0 \cdot 7457 \dots$ So \$1 = £0 \cdot 7457 \dots £200 \dots 0 \cdot 7457 \dots = 268 \cdot 18 \dots = [\$] 268 \cdot 18 [2 D.P.]	

Q4	Model Solution – 15 Marks	Marking Notes
(a)	{1, 2, 3, 4, 6, 12}	 Scale 5C (0, 2, 3, 5) Accept correct answer without supporting work Note: If incorrect excess factors are given, award at most <i>High Partial Credit</i> <i>Low Partial Credit</i> One correct factor. <i>High Partial Credit</i> <i>Sour correct factor</i>
(b)	F	 Scale 10C (0, 3, 7, 10) Accept correct answer without supporting work. Ignore any elements in Venn diagram placed outside set F If a region contains an incorrect element, award at most HPC. If an element is written twice in F then that element is not correctly placed If answer from (a) has elements in 3 regions, FC may be awarded for (b); if answer from (a) only has elements in 2 regions, award at most HPC for (b); if answer from (a) only has elements in 1 region, award at most LPC for (b). Low Partial Credit 1 region with all relevant elements (with or without excess elements) 3 elements correctly placed High Partial Credit 2 regions with all relevant elements and no excess 5 elements correctly placed

Q5	Model Solution – 25 Marks	Marking Notes
(a)	$3(6) - 4(5^{2})$ $= 18 - 4(25)$ $= 18 - 100$ $= -82$	 Scale 5B (0, 3, 5) Accept correct answer without supporting work Partial Credit Some correct substitution or relevant
(b)	$= 2x(4-5x+x^{2}) - 3(4-5x+x^{2})$ = $8x - 10x^{2} + 2x^{3} - 12 + 15x - 3x^{2}$ = $2x^{3} - 13x^{2} + 23x - 12$	calculation. Scale 10D (0, 2, 6, 9, 10) Low Partial Credit • One term correctly multiplied Mid Partial Credit • Three terms correctly multiplied High Partial Credit • 2nd line fully correct
		 4 terms correct in 2nd line, finished correctly Correct answer without supporting work
(c)	$10de - df - 5ef + 2d^{2}$ $= 10de - 5ef + 2d^{2} - df$ $= 5e(2d - f) + d(2d - f)$ $= (2d - f)(5e + d)$	 Scale 10C (0, 3, 7, 10) Low Partial Credit Work of merit, for example: a common factor identified from given expression
	OR $10de - df - 5ef + 2d^2$ $= 10de + 2d^2 - 5ef - df$ = 2d(5e + d) - f(5e + d) = (5e + d)(2d - f)	 High Partial Credit 5e(2d - f) + d(2d - f) or equivalent Correct answer without supporting work 5e(2d - f) - d(2d - f) or similar, and finishes correctly.

Q6	Mod	Model Solution – 40 Marks Marking Notes	
(a) <i>,</i>	(a)	16, 32, 64	Scale 10C (0, 3, 7, 10)
(b)	(b)	Domain: {1, 2, 3, 4, 5, 6} Range: {2, 4, 8, 16, 32, 64}	 Accept correct answers without supporting work. Accept answers in index form (2⁴, 2⁵, 2⁶) Low Partial Credit Work of merit in (a) or (b), for example: in (a), one correct entry; indicates doubling; indication of 2¹, 2², or 2³; in (b), three correct entries in either domain or range; or full domain in place of range; or full range in place of domain (but see note below regarding FC-1) High Partial Credit (b) correct (a) correct and work of merit in (b) Full Credit –1
			 Apply a * for domain and range correct but swapped
(c),	(c)	2, 4, 8, 16, 32, 64, 128, 256, 512	Scale 10D (0, 2, 6, 9, 10)
(d)		i.e. 9 [folds]	Accept correct answers without supporting work.
	(d)	512, 1024, 2048, 4096	Consider solution as requiring 3 steps:
		i.e. $4.096 imes 10^3$ [layers]	Step 1: solves part (c)
		OR	Step 2: finds 4096 in part (d)
		$2^{12} = 4096$	Step 3: writes answer for (d) in correct form.
		$= 4.096 \times 10^3$ [layers]	 Low Partial Credit Work of merit in (c) or (d), for example: some correct continuation of candidate's pattern from (a); divides 500 by 2 (in (c)); some relevant use of 2^x
			 Mid Partial Credit 1 step correct (including expressing any number relevant to their solution in the form a × 10ⁿ)
			High Partial Credit2 steps correct

Q6	Model Solution – 40 Marks	Marking Notes
(e), (f)	 (e) There will be more than 10 000 layers after 14 folds <i>or any other valid explanation</i> (f) <i>Answer</i>: Exponential <i>Reason</i>: It doubles each time OR The first differences are the same as the original sequence OR The variable is a power 	 Scale 10D (0, 2, 6, 9, 10) Low Partial Credit Work of merit in (e) or (f), for example: in (e), mentions 14 folds or 10 000 layers; in (f), correct box ticked; or shows understanding of linear / quadratic / exponential pattern. Mid Partial Credit (e) or (f) correct Work of merit in (e) and (f) High Partial Credit One part correct and work of merit in the other part
	or any other valid reason	
(g) <i>,</i> (h)	(g) $k \times 2 \times 2 \times 2 = 8k$ (h) $2^{p} \times 2 \times 2 \times 2$ $= 2^{p} \times 2^{3} = 2^{p+3}$	 Scale 10C (0, 3, 7, 10) Accept correct answers without supporting work. If a particular value is used for k or 2^p or p, award LPC at most, even if relevant work is presented in both (g) and (h) Low Partial Credit: Work of merit in (g) or (h), for example: indicates multiplication by 2; indicates 8 in (g) High Partial Credit (g) or (h) correct. Work of merit in both (g) and (h)

Q7	Model Solution – 15 Marks		Marks	Marking Notes
(a)	Nur €5 or with	nber of notes 3 5 h Way 2 = (Number of €2 coins 6 1 (5, 1) and Way 3 = (3, 6)	 Scale 5C (0, 2, 3, 5) Accept correct answers without supporting work. Low Partial Credit Some work of merit, for example: attempt at trial and improvement High Partial Credit One way correct
(b)	All even numbers can be made using $\notin 2$ coins. $\notin 5$ is the smallest odd number which can be made. All remaining odd numbers can be made using a $\notin 5$ note and the required number of $\notin 2$ coins. OR No $\notin 2$: 5, 10, 15, = all no's ending in 0 or 5 One $\notin 2$: 7, 12, 17, = all no's ending in 2 or 7 Two $\notin 2$: 4, 9, 14, = all no's ending in 4 or 9 Three $\notin 2$: 6, 11, 16, = all no's ending in 6 or 1 Four $\notin 2$: 8, 13, 18, = all no's ending in 8 or 3 OR 2k gives all even 5 + 2k gives all odd OR		<pre>be made using €2 coins. I number which can be mbers can be made using a ired number of €2 coins. OR = all no's ending in 0 or 5 = all no's ending in 2 or 7 = all no's ending in 4 or 9 = all no's ending in 6 or 1 = all no's ending in 8 or 3 OR ves all even gives all even gives all odd OR r valid explanation</pre>	 Scale 10C (0, 3, 7, 10) Accept indication of how to make all possible values, without full explanation. Low Partial Credit Some work of merit, for example: gives one way of making an amount other than €2 or €5 High Partial Credit Shows how to make all values in one infinite subset of the natural numbers that are greater than 3, for example: all even numbers; or all (relevant) odd numbers; or all multiples of five

Q8	Model Solution – 25 Marks	Marking Notes
(a)	$x = \frac{-(-4)\pm\sqrt{(-4)^2 - 4(1)(-7)}}{2(1)}$ = $\frac{4\pm\sqrt{16+28}}{2}$ = $\frac{4\pm\sqrt{44}}{2}$ = $5 \cdot 316$ or $-1 \cdot 316$ = $5 \cdot 32$ or $-1 \cdot 32$ [2 D.P.]	 Scale 15C (0, 4, 12, 15) Note: If one root is given, award HPC at most Consider the solution as having 3 steps: Step 1: Correct formula Step 2: Full correct substitution into the quadratic formula. Step 3: Evaluates the quadratic formula.
		 Low Partial Credit 1 step correct Identifies a, or b, or c Correctly factorised and stops 1 correct answer without work High Partial Credit 2 steps correct 2 correct answers without work Full Credit −1 Apply a * for incorrect rounding, or for answers in surd form: 2 + √11, 2 - √11
(b)	Answer: A Justification: It is the only one that crosses the y-axis at -2 [and $f(0) = -2$] OR Not C because the roots are wrong, and not B because the y-intercept is wrong.	 Scale 10C (0, 3, 7, 10) If multiple boxes are ticked, ignore all ticks (unless answer is clearly identified) Award FC if candidate inputs an x value into f (x) and generates the corresponding y value that uniquely defines graph A. Low Partial Credit Correct graph identified Work of merit in justification, for example: explains why it is not B or C; shows understanding that graph crosses x-axis at roots High Partial Credit Correct graph identified and work of merit in justification

Q9	Model Solution – 25 Marks	Marking Notes
(a)	$\frac{45}{15} \times 10\ 000 = 30\ 000$ [views]	 Scale 5B (0, 3, 5) Accept correct answer without supporting work. Partial Credit Work of merit, for example, some correct multiplication or division indicated including reciprocals
(b), (c)	(b) $\frac{80\ 000}{10\ 000} \times 15 = [€]120$ (c) $\frac{15}{10\ 000} = [€]0.0015$ OR $[€]1.5 \times 10^{-3}$ OR $[€]\frac{3}{2000}$	 Scale 5D (0, 2, 3, 4, 5) Accept correct answers without supporting work. Accept correct answers in euro, without unit. Low Partial Credit Work of merit in (b) or (c), for example, some correct multiplication or division indicated, including reciprocals Mid Partial Credit (b) or (c) correct Work of merit in both (b) and (c) High Partial Credit (b) or (c) correct and work of merit in the other part Full Credit -1 Correct answer(s) given in cent (with unit)
(d)	Profit = Revenue - Cost [€] 0·0015 <i>x</i> — 70	 Scale 5B (0, 3, 5) Accept correct answer without supporting work. Partial Credit One correct term in expression, for example: -70 Correct relevant formula: Profit = Revenue - Cost

Q9	Model Solution – 25 Marks	Marking Notes
(e)	(i) $\frac{0.0015x-70}{7} = 200$	Scale 10D (0, 2, 6, 9, 10)
	OR	In (ii), correct answer without work is considered work of merit (rather than correct)
	(ii) $0 \cdot 0015x - 70 = 1400$ $0 \cdot 0015x = 1470$	<i>Note</i> : in (ii), candidate must deal adequately with the 15 and the 10 000, otherwise it is considered at most work of merit in (ii).
	$x = 980\ 000$	 Low Partial Credit Work of merit in (i) or (ii), for example: (i) 7 × 200 ; (ii) 1470, or ÷ 15, or × 10 000
		 <i>Mid Partial Credit</i> (i) or (ii) correct Work of merit in (i) and (ii)
		<i>High Partial Credit</i>One part correct and work of merit in the other part
		 Full Credit –1 Apply a * for the -70 missing or misused in (e)



Q10	Model Solution – 30 Marks	Marking Notes
(b)	When $x = 35\ 000$, $y = 0 \cdot 2 \times 35000 = 7000$ When $x = 60\ 000$, Balance $= 60\ 000 - 35\ 000 = 25\ 000$, so $y = 7000 + (0 \cdot 4 \times 25000)$ $= 7000 + 10\ 000 = 17\ 000$	Scale 10C (0, 3, 7, 10) Accept correct answer without supporting work. Tolerance: 1,000 on x-axis and 500 on y-axis Note: Graph must have a change of slope at $x = 35\ 000$ for Full Credit <i>Low Partial Credit</i> • Some correct relevant calculation • Given line continued correctly for one box • Plots (50 000, 13 000) or (35 000, 7 000) <i>High Partial Credit</i> • One section of graph correct, that is: given line continues until $x = 35\ 000$ and stops; or correct line drawn from $x = 35\ 000$ to $x = 60\ 000$ • Graph correct below $x = 30\ 000$ and from $x = 40\ 000$ up to $x = 60\ 000$
(c)	See dotted line graph above.	 Scale 5B (0, 3, 5) Note: if incorrect graph is given in (b) in the domain [15 000, 60 000], award FC in (c) if it is shifted correctly. Partial Credit Graph in (b) (over a domain of width at least 10 000) shifted vertically or horizontally Some relevant calculation Two points plotted correctly

Q11	Model Solution – 10 Marks	Marking Notes
	$-3 \le x \le 1, \qquad x \in \mathbb{Z}$	Scale 10D (0, 2, 6, 9, 10)
	or anv other valid inequality	 Low Partial Credit Work of merit, for example: One correct box ticked;
	$r < 3$ $r \in \mathbb{N}$	one inequality partially correct.
		Mid Partial Credit
	$0 \cdot 5 < x < 4, x \in \mathbb{Z} \text{ or } x \in \mathbb{N}$	 One part fully correct (inequality and matching domain)
		• Two inequalities correct, but incorrect or no box(es)
	or any other valid inequality	ticked
	$-2 < x < 4, \ x \in \mathbb{R}$	High Partial Credit
		 Two parts fully correct (inequality and matching domain)
		 Three inequalities correct, but incorrect or no box(es) ticked
		 Full Credit –1 Apply a * the first time the strictness of an inequality is incorrect; ignore any subsequent such errors

Q12	Model Solution – 15 Marks	Marking Notes
(a)	$\frac{2}{n-3} - \frac{5}{2n+5}$ $= \frac{2(2n+5) - 5(n-3)}{(n-3)(2n+5)}$ $= \frac{4n+10 - 5n+15}{(n-3)(2n+5)}$ $= \frac{-n+25}{(n-3)(2n+5)}$ OR $= \frac{-n+25}{2n^2 - n - 15}$	 Scale 10D (0, 2, 6, 9, 10) Low Partial Credit Work of merit , for example: Correct common denominator; some correct multiplication implied in numerator 2(n-3)-5(2n+5) (n-3)(2n+5) and continues Mid Partial Credit Numerator set up correctly and denominator correct Two terms correct out of 4n + 10 – 5n + 15 in numerator and finishes correctly No or incorrect common denominator but numerator correct as per solution High Partial Credit 4n+10-5n+15 (n-3)(2n+5) 3 terms correct in numerator and finishes correctly Correct answer without supporting work Full Credit -1 Shows common denominator as denominator in calculations but then drops it subsequently
(b)	$(4x-3)^{2} + 24x$ = $16x^{2} - 12x - 12x + 9 + 24x$ = $16x^{2} - 24x + 9 + 24x$ = $16x^{2} + 9$, and $x^{2} \ge 0$ so $16x^{2} + 9 > 0$	Scale 5C (0, 2, 3, 5) Low Partial Credit • Correctly evaluates the expression for one real value of x • $(4x - 3)(4x - 3)$ High Partial Credit • One correct term in multiplication of given expression • Indication that $()^2 \ge 0$ Full Credit -1 • $16x^2 + 9$, but with no conclusion

Q13	Model Solution – 15 Marks	Marking Notes
Q13 (a), (b)	Model Solution – 15 Marks (a) 1 Sometimes true 2 Never true 3 Always true 4 Always true (b) Gives two examples: one where statement is true and one where statement is not true. For example: True for {1, 2} and {3, 4}; False for {1, 2} and {1, 3}. OR True if $P = 7$ days of the week and Q = months of year; False if $P = 7$ days of the week and Q = days of the week and Q = days of the week and Q = days of the week end Q = days of the week end	 Marking Notes Scale 15D (0, 3, 9, 13, 15) Low Partial Credit One statement correct in (a) No statements correct in (a) but work of merit in (b), for example: answers "Always True" for Statement 1 and gives example where it is true Mid Partial Credit Two statements correct in (a) and work of merit in (b), for example: Statement 1 correct and gives example where it is true (or where it is false) High Partial Credit All four statements correct in (a) Three statements correct in (a) and work of merit in (b) One statement correct in (a)
	States "True if $P \cap Q = \emptyset$, otherwise false."	
	or any other valid justification	

Q14	Model Solution – 25 Marks	Marking Notes
(a)	$= \frac{\frac{(2n-5)(n+3)}{(n+3)(n-3)}}{\frac{2n-5}{n-3}}$	 Scale 15C (0, 4, 12, 15) Low Partial Credit Work of merit in numerator or denominator, for example: guide number correctly identified in top line (-30 or 30)
		 High Partial Credit Numerator or denominator factorised correctly Correct answer without work
(b)	(i) $(x + a)(x + b) = 0$ x + a = 0 or x + b = 0 x = -a or x = -b (ii) $(x + a)(x + b) \div (x + a)$ = x + b	 Scale 10C (0, 3, 7, 10) Accept correct answer without supporting work. Low Partial Credit Work of merit in (i) or (ii), for example: replaces x² + (a + b) x + ab with (x + a)(x + b) One correct term in answer if using long division in (ii) High Partial Credit
		 (i) or (ii) correct Work of merit in (i) and (ii)

Paper 2

Structure of the marking scheme

Candidate responses are marked according to different scales, depending on the types of response anticipated. Scales labelled A divide candidate responses into two categories (correct and incorrect), scales labelled B divide responses into three categories (correct, partially correct, and incorrect), and so on. The scales and the marks that they generate on this examination paper are summarised in this table:

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15-mark scale		0, 6, 10, 15	0, 5, 9, 12, 15
20-mark scale			0, 5, 10, 15, 20

A general descriptor of each point on each scale is given below. More specific directions in relation to interpreting the scales in the context of each question are given in the scheme, where necessary.

Marking scales – level descriptors

B-scales (three categories)

- response of no substantial merit (no credit)
- partially correct response (partial credit)
- correct response (full credit)

C-scales (four categories)

- response of no substantial merit (no credit)
- response with some merit (low partial credit)
- almost correct response (high partial credit)
- correct response (full credit)

D-scales (five categories)

- response of no substantial merit (no credit)
- response with some merit (low partial credit)
- response about half-right (mid partial credit)
- almost correct response (high partial credit)
- correct response (full credit)

In certain cases, typically involving incorrect rounding, omission of units, a misreading that does not oversimplify the work, or an arithmetical error that does not oversimplify the work, a mark that is one mark below the full-credit mark may be awarded. This level of credit is referred to as *Full Credit* -1, and these types of errors are identified with an asterisk (*). Thus, for example, in Scale 10C, *Full Credit* -1 of 9 marks may be awarded.

No marks may be awarded other than those on the appropriate scale, and *Full Credit* -1.

Question 1 (15)		Question 6 (40)		Question 10 (35)	
(a) <i>,</i> (b)	10C	(a)	5C	(a)	15C
(c)	5B	(b),(c)	10D	(b)	15C
		(d)	10C	(c)	5B
Question 2	2 (25)	(e)	10C		
(a)	5B	(f)	5B	Question :	11 (15)
(b)	10D	• • •	- (20)		15D
(c)	10C	Question	7 (30)		
(-)		(a)	15D	Question :	12 (30)
$O_{\text{constinue}} = 2 (20)$		(b)(i)	10D	(a)	5B
Question :	5 (50)	(b)(ii)	5C	(a) (b)	50
(a)	10C			(\mathbf{c})	200
(b)	10C	_	- ()	(C)	200
(c)	10D	Question	8 (10)		
			10C	Question 2	13 (15)
Question 4	4 (25)			(a)	5B
(a) <i>,</i> (b)	10D	Question	9 (10)	(b)	10D
(c)	10C		100		
(d)	5C		100	Question 2	14 (5)
					5D
Question 5 (15)					

Summary of mark allocations and scales to be applied

(a) 10D (b),(c) 5D

Model Solutions & Marking Notes

The model solutions for each question are not intended to be exhaustive – there may be other correct solutions. Any Examiner unsure of the validity of the approach adopted by a particular candidate to a particular question should contact his / her Advising Examiner.

Where the scheme refers to "work of merit", examples are given of the standard acceptable as work of merit in that particular part.

In general, accept a candidate's work in one part of a question for use in subsequent parts of the question, unless this oversimplifies the work involved.

Q1	Mod	el Solution – 15 Marks	Marking Notes		
Q1 (a), (b)	Mod (a) (b)	el Solution – 15 Marks $X = 40^{\circ}$ Triangle AOD is isosceles $Y = \frac{180-40}{2} = \frac{140}{2} = 70^{\circ}$ OR angle BOD = 2Y 140 = 2Y	Marking NotesScale 10C (0, 3, 7, 10)Accept correct answers without work.Accept correct answers given on diagram.Low Partial Credit• (a) correct• Work of merit in (b), for example: indicates that AOD is isosceles;		
	$\mathbf{Y} = 70^{\circ}$	mentions 180°; indicates that exterior angle equals sum of interior opposite angles;			
			<i>High Partial Credit</i>(a) correct and work of merit in (b)		
			• (b) correct		
			 Full Credit -1 Apply a * for no or incorrect units Apply it only the first time it occurs (in (a) or in (b)) 		

Q1	Model Solution – 15 Marks	Marking Notes
(c)	$Y + Z = 180^{\circ}$ [opposite angles in a cyclic quadrilateral] $Z = 180 - 70 = 110^{\circ}$ OR 2Z = reflex angle BOD 2Z = 220 $Z = 110^{\circ}$	 Scale 5B (0, 3, 5) Accept correct answer without work. Accept correct answer on diagram for work. Partial Credit Work of merit, for example: correct relevant statement about cyclic quadrilateral ABCD; angle at the centre is twice angle at the circumference; mentions 140° or 220°; extends [OA] beyond A Full Credit –1 Apply a * for no or incorrect units, if it has not already been applied in (a) or (b)

Q2	Model Solution – 25 Marks	Marking Notes
(a)	Volume = $5 \times 14 \times 24$	Scale 5B (0, 3, 5)
	$= 1680 [\text{cm}^3]$	Accept correct answer without work.
		Accept correct answer without units.
		Partial Credit
		Correct volume formula
		• Finds the area of one face
(b)	Height: $(4 \times 5) + 2 = 22$ [cm]	Scale 10D (0, 2, 6, 8, 10)
		Accept correct answers without work.
	Width: $(3 \times 14) + 2 = 44$ [cm]	Accept correct answers without units.
		Low Partial Credit
	Length: $(3 \times 24) + 2 = 74$ [cm]	 Some correct relevant calculation
		Mid Partial Credit
		 One dimension (including the cover) correctly calculated
		 Two dimensions correct, with the cover ignored or mishandled
		High Partial Credit
		 Two dimensions (including the cover) correctly calculated
		• Three dimensions correct, with the cover ignored or mishandled
		Full Credit – 1
		Apply a * for answers in incorrect boxes

(c)Total volume including plastic, minus total volume excluding plastic:Scale Low I $(22 \times 44 \times 74) - (36 \times 1680)$ • W $= 71632 - 60480$ co $= 11152 \text{ cm}^3$ a I	le 10C (0, 3, 7, 10) [,] Partial Credit
OROR $22 \times 44 \times 2 = 968 \times 2 \times 1 = 1936$ $+ 22 \times 72 \times 2 = 1584 \times 2 \times 1 = 3168$ $+ 42 \times 72 \times 2 = 3024 \times 2 \times 1 = 6048$ $= 11 152 \text{ cm}^3$ • Fin 	Nork of merit, for example: correct area/volume formula; calculates i relevant volume (other than that in part (a)) 36×1680 <i>h Partial Credit</i> inds total volume including cover 71 632) or total volume excluding cover 60 480) inds volume of plastic cover correctly put mishandles edges and/or corners, for example: finds total surface area ncluding cover (11 704) or total surface area excluding cover (10 608) Correct answer without work <i>Credit –1</i> Apply a * for no or incorrect units

Q3	Model Solution – 30 Marks	Marking Notes
(a)	$l^{2} = r^{2} + h^{2}$ $l^{2} = 5^{2} + 12^{2}$ $l^{2} = 25 + 144$ $l^{2} = 169$ $l = 13 \text{ cm}$	 Scale 10C (0, 3, 7, 10) Accept correct answer without work. Low Partial Credit Correct formula
		 <i>High Partial Credit</i> <i>l</i>² = 169
		• One error and finishes correctly, for example: $l = \sqrt{34}$; $l = \sqrt{119}$
		 Full Credit -1 Apply a * for no or incorrect units
(b)	TSA = $\pi(5)(13) + \pi(5)^2$	Scale 10C (0, 3, 7, 10)
	$= 65\pi + 25\pi = 90\pi$	Accept correct answer without units.
	= $282 \cdot 74 \text{ [cm^2]}$ = $282 \cdot 7 \text{ [cm^2]}$ [1 D.P.]	 Low Partial Credit A correct relevant formula (curved surface area or area of circle)
		Total surface area of cylinder formula
		High Partial CreditFully correct substitution into correct formulae
		Finds curved surface area only
		 One error and finishes correctly, for example, total surface area of a cylinder
		Correct answer without work
		 Full Credit – 1 Apply * for 90π Apply * for no or incorrect rounding

Q3	Model Solution -	- 30 Marks	Marking Notes
(c)	Circle:		Scale 10D (0, 2, 6, 8, 10)
	Radius of circle	= 5 [cm]	Accept correct answers without units.
	Circumference	$= 2\pi(5) = 31.41$	Accept correct answers without work.
		= 31·4 [cm] [1 D.P.]	Accept correct answers in incorrect or no boxes for up to <i>High Partial Credit.</i>
	Sector:		A length measured from the diagram of the
	Radius of Sector	= 13 [cm]	net is not considered correct.
	Length of Arc	= 31·4 [cm]	Low Partial CreditSome correct relevant calculation indicated
			Correct relevant formula
			One measurement correct
		<i>Mid Partial Credit</i>Two measurements correct	
		<i>High Partial Credit</i>Three measurements correct	
			 Full Credit – 1 Apply a * for no or incorrect rounding, once only

Q4	Model Solution – 25 Marks			Marking Notes
(a),	(a) $P(Win) = \frac{1}{3}$			Scale 10D (0, 2, 6, 8, 10)
(b)				Accept correct answers without work.
				Low Partial Credit
				• (a) correct
	WW WD	WL	One correct entry in (b)	
	DW	DD	DL	Mid Partial Credit
	LW	LD	LL	 (a) correct and three correct entries in (b) five correct entries in (b)
				All eight entries in (b) listed
				High Partial Credit
				• (a) correct and five correct entries in (b)
				• (a) correct and all eight entries in (b) listed
				• (b) correct
				Full Credit – 1
				 Apply a * for (a) correct and all eight entries in (b) reversed
(c)	(i) $P(WL) = \frac{1}{9} \text{ or } 0 \cdot 11 \dots$			Scale 10C (0, 3, 7, 10)
	9			Accept correct answers without work.
	(ii) P(at leas	t one W) = $\frac{3}{2}$	⁵ or 0 · 55	Low Partial Credit
			2	• Work of merit in (i) or (ii), for example:
				correct numerator or denominator;
				lists some or all relevant outcomes;
				use of some relevant fraction, for example $\frac{1}{3}$
				High Partial Credit
				• (i) or (ii) correct
				Full Credit – 1
				Apply a * for no indication of recurrence

Q4	Model Solu	ition – 25 Marks	Marking Notes
(d)	(i)		Scale 5C (0, 2, 3, 5) Accept correct answers without work.
	Total outco	$mes = 3 \times 3 \times 3 = 27$	
	Lists: WM WD WLV DW Answer = 2 (ii) P(doesn't v	OR WWWDWWL WWDWUL WUDWLL WDWD 27 win) = $\frac{2^3}{27} = \frac{8}{27}$	 Low Partial Credit Work of merit in (i) or (ii), for example: lists some relevant outcomes in either part; correct numerator or denominator in (ii) High Partial Credit (i) or (ii) correct Work of merit in (i) and (ii)
	Lists: DDI DDL DLD DLL Answer = $\frac{1}{2}$	OR LDD LDL LLD LLL 8 27	

Q5	Model Solution – 15 Marks	Marking Notes
(a)	(i) Range = $15 - 3 = 12$ [minutes]	Scale 10D (0, 2, 6, 8, 10)
		Accept correct answers without work.
	(ii) $Q_1 = \frac{6+7}{2} = 6 \cdot 5$	Accept correct answers without units.
	$Q_3 = \frac{13 + 14}{2} = 13 \cdot 5$ IQR = 13 \cdot 5 - 6 \cdot 5 = 7	Accept any value of Q_1 in the range $6 \le Q_1 \le 7$, and any value of Q_3 in the range $13 \le Q_2 \le 14$. However, if the IQR is not being given as 7, work must be shown in order for it to be considered correct.
		In order to be considered correct, both the range and IQR must be given as values rather than as intervals.
		 Low Partial Credit Work of merit in (i) or (ii), for example: identifies min or max; indicates Q1 or Q3
		Mid Partial Credit (i) correct
		• Work of merit in (i) and (ii)
		• Finds value of Q1 and Q3
		<i>High Partial Credit</i>(i) correct and finds value of Q1 and Q3
		• (ii) correct
		 (i) and (ii) both given as intervals, otherwise correct
(b),	(b) $\frac{1}{7}$ of Range: B	Scale 5D (0, 2, 3, 4, 5)
(c)	$\frac{1}{2}$ of Range: A	Low Partial CreditOne correct entry in (b)
	$\frac{3}{4}$ of Range: C	 Work of merit in (c), for example: some relevant reference to the spread of data; reference to the middle 50%
	Most of the data is grouped near the middle, so the middle 50% will be squashed into the smallest interval	 Mid Partial Credit One correct entry in (b) and work of merit in (c)
	[relative to the range]	<i>High Partial Credit</i>(b) correct
	or any other valid justification	 Histogram B correct in table and (c) correct

Q6	Model Sol	ution	- 40	Marks		Marking Notes			
(a)	Mean = $\frac{sur}{1}$	$\frac{m}{1} = \frac{1}{1}$	$\frac{22 \cdot 2}{14} =$	8.72	= 8	3∙7 kg	[1 D.	P.]	Scale 5C (0, 2, 3, 5)
	14	ł	14				Accept correct answer without work.		
									 Low Partial Credit Work of merit, for example: indicates division by 14, indicates sum of values
									High Partial Credit • $\frac{122\cdot 2}{14}$
									Full Credit –1
									 Apply a * for no or incorrect units
									 Apply a * for no or incorrect rounding
(b),	(b)								Scale 10D (0, 2, 6, 8, 10)
(c)	Girls:	1	2	2	3	7	0	1	Low Partial Credit
	Boys:	1	1	1	4	6	1	0	• Work of merit in (b) or (c), for
									example: in (b) 4 correct values:
	(c)								in (c), answer correct;
	Answer:			_					work of merit in justification
	No, Eoin is	s not o	correc	t.					<i>Mid Partial Credit</i>Work of merit in (b) and (c)
	Reason:								• (b) or (c) correct
	The mean	s are	rough	ly the	same				Hiah Partial Credit
				OR					• (b) or (c) correct, and work of
	The boys'	mear	n is slig	htly b	igger				merit in the other part
				OR					Full Credit –1
	The distrik similar	outior	ns in th	ne frec	quenc	y tabl	e are v	very	 Apply a * for one incorrect entry in (b), otherwise correct
		or	any ot	her va	lid re	ason			



Q6	Model Solution – 40 Marks	Marking Notes
(e)	$\frac{(2 \cdot 5 \times 5) + (7 \cdot 5 \times 4) + (15 \times 7) + (25 \times 8) + (40 \times 3) + (75 \times 1) + (125 \times 2)}{30}$ = $\frac{12 \cdot 5 + 30 + 105 + 200 + 120 + 75 + 250}{30}$ = $\frac{792 \cdot 5}{30} = 26 \cdot 416 \dots$ = $[\pounds] 26 \cdot 42$ [nearest cent]	 Scale 10C (0, 3, 7, 10) Accept correct answer without work. Accept correct answer without units. Accept use of 0 - 4.99, 5 - 9.99, etc. Low Partial Credit Work of merit, for example: indicates division by 30; one correct mid-interval value; numerator with consistent incorrect mid-interval values
		 High Partial Credit Consistent incorrect mid-interval values, finished correctly Numerator correct, whether evaluated to 792 · 5 or not One error and finishes correctly Full Credit –1 Apply a * for no or incorrect rounding
(f)	Median = mean of 15 th and 16 th values Last 2 people in 10 – 20 class are 15th and 16th, so median is between them. For example, [€] 18 · 50.	 Scale 5B (0, 3, 5) Accept any subset of the interval [15 – 20] for <i>Full Credit</i>. Accept correct answer without euro symbol. <i>Partial Credit</i> Work of merit, for example: shows understanding of median as middle value <i>Full Credit – 1</i> Apply a * for 10 – 20 class identified Apply a * for answer with no justification

Q7	Model Solution –	30 Marks	Marking Notes
(a)	(i) Angle	= 90°	Scale 15D (0, 5, 9, 12, 15)
			Accept correct answers without work.
	(ii) slope	of $n = -\frac{5}{2}$	Low Partial Credit
	Fan: $v - (-)$	$x = -\frac{5}{2}(x-6)$	 Work of merit in (i) and/or (ii),
	-9 9 (-	2	in (i), mentions right angle:
			in (ii), finds slope of <i>n</i> ;
			correct relevant formula ($y = mx + c$ or
			$y - y_1 = m(x - x_1)$)
			Mid Partial Credit
			• (I) or (II) correct
			High Partial Credit
			other part
			Full Credit –1
			 Apply a * for no or incorrect units in (i)
(b)	Line Slop	e Point	Scale 10D (0, 2, 6, 8, 10)
(i)	k 1	(0, -1)	Accept correct answers without work.
	$l \qquad \frac{2}{3}$	(0, -2)	Low Partial Credit
			• Work of merit towards finding one value, for example: $y = mx + c$: $x = 0$
			One correct entry in table
			Mid Partial Credit
			Two correct entries in table
			High Partial Credit
			Three correct entries in table
			Full Credit –1
			 Apply a " If the point(s) where the line crosses the v-axis are given as a value (-1)
			or -2) instead of a point, or if the
			co-ordinates are reversed, once only

Q7 Model Solution – 30 Marks	Marking Notes
Q7 Model Solution - 30 Marks (b) $y = x - 1$ (ii) $xo 2x - 3(x - 1) = 6$ xo -x + 3 = 6 xo x = -3 x = -3 x = -3 x = -3 x = -4 Answer: $(-3, -4)$ OR x - y = 1 2x - 3y = 6 xo -2x + 2y = -2 2x - 3y = 6 $x - y = 4 \rightarrow y = -4$ x = -3 Answer: $(-3, -4)$	 Marking Notes Scale 5C (0, 2, 3, 5) Accept "x = -3 and y = -4" for Full Credit. Low Partial Credit Work of merit in solving the simultaneous equations algebraically, for example: substitution of x - 1 into second equation; rearranges one equation Correct answer without work or based on construction High Partial Credit Solves for one variable (x = -3 or y = -4) with supporting algebraic work One error and finishes correctly Correct answer with some (non-algebraic) justification, for example: subbed into both equations; reasoning based on y-intercepts and slopes

Q8	Model Solution – 10 Marks	Marking Notes	
	Answer:	Scale 10C (0, 3, 7, 10)	
	51	Low Partial Credit	
	Justification:	• Work of merit, for example:	
	Slope = -2	finds another point on the line;	
	So for every unit across we drop 2 units. So positive integer <i>y</i> -values are: 101, 99, 97,, 1.	understanding of meaning of slope in context	
	There are 51 odd numbers between 0 and 101 inclusive.	<i>High Partial Credit</i>Finds equation of line	
	OR	 Indicates relevance of odd numbers 	
	Equation: $y - 101 = -2(x - 1)$	One error and finishes correctly	
	so $y = -2x + 103$	Correct answer without work	
	Cuts x-axis when $y = 0$, so $x = 51 \cdot 5$.	Full Credit –1	
	So required points are when $x = 1$ to 51, inclusive	 Apply a * if (0, 103) is included 	
	[as all of these points have positive integer y-values]		
	or any other valid justification		

Q9	Model Solution – 10 Marks		Marking Notes	
	2. QT = ST		Scale 10D (0, 2, 6, 8, 10)	
	3. 4.	angles opposite equal sides in an isosceles triangle are equal QK = SK	A statement/reason may be accepted as correct even if the previous statements/reasons are not correct.	
	5.	SAS [Side Angle Side]	Low Partial CreditOne statement/reason correct	
	or any other valid and appropriate statements / reasons		<i>Mid Partial Credit</i>Two statements/reasons correct	
			<i>High Partial Credit</i>Three statements/reasons correct	

Q10	Model Solution – 35 Marks	Marking Notes
(a)	$2 \cdot 1 \div 0 \cdot 175 = 12$ steps	Scale 15C (0, 6, 10, 15)
	$12 \times 0 \cdot 25 = 3$ metres	Accept 12 risers and 11 treads
	OR	[i.e. top riser has no associated tread], so sum of treads = $11 \times 0 \cdot 25 = 2.75$ metres
2	$\frac{x}{2 \cdot 1} = \frac{250}{175}$ $x = \frac{2 \cdot 1(250)}{175} = 3 \text{ metres}$	 Low Partial Credit Work of merit, for example: identifies correct tread or riser; some relevant calculation, even if using an incorrect tread and/or riser value from table
		High Partial Credit • A correct relevant ratio, for example: $\frac{2 \cdot 1}{0 \cdot 175}, \frac{250}{175}$ or equivalent
		 Uses incorrect tread and/or riser value from table, but finishes correctly
		Correct answer without work
		 Full Credit –1 Apply a * for no or incorrect units

Q10	Model Solution – 35 Marks	Marking Notes
(b)	$\tan A = \frac{2 \cdot 1}{3} = \frac{175}{250} = \frac{7}{10}$ $A = \tan^{-1} \frac{7}{10}$ $A = 34 \cdot 9 \dots = 35^{\circ} \text{ [nearest degree]}$ \mathbf{OR} $x^{2} = \sqrt{175^{2} + 250^{2}} = \sqrt{93} 125$ $\sin A = \frac{175}{\sqrt{93} 125} = 0 \cdot 573 \dots$ $A = 34 \cdot 9 \dots = 35^{\circ} \text{ [nearest degree]}$ \mathbf{OR} $x^{2} = \sqrt{175^{2} + 250^{2}} = \sqrt{93} 125$ $\cos A = \frac{250}{\sqrt{93} 125} = 0 \cdot 819 \dots$ $A = 34 \cdot 9 \dots = 35^{\circ} \text{ [nearest degree]}$	 Scale 15C (0, 6, 10, 15) Accept correct answer with no units. Low Partial Credit Work of merit, for example: correctly identifies opposite or adjacent sides; identifies a correct measurement on diagram; identifies A in small triangle on given diagram A correct trigonometric ratio Incorrect trigonometric ratio, for example: tan A = 10/7 or cos A = 175/250, and finishes correctly High Partial Credit A correct trigonometric ratio fully subbed in tan A = 2·1/2 and finishes correctly (37 · 3 = 37° [nearest degree]) Correct answer with no work Full Credit -1 Apply a * for no or incorrect rounding Apply a * if the answer is given in radians (0 · 6 = 1 [nearest unit]) or credients (22 · 9 = 20 [nearest unit])
(c)	Tread = 280 [mm] Riser = 180 [mm]	 Scale 5B (0, 3, 5) Accept correct answers without units. Partial Credit Tread or riser correct. Tread and riser correct for a private building (Tread = 220 mm and Riser = 220 mm) Full Credit -1 Apply a * for answers swapped (Tread = 180; Riser = 280)

Q11	Model Solution – 15 Marks	Marking Notes	
Q11	Model Solution – 15 Marks $\cos F = \frac{6}{11} = \frac{\text{adj}}{\text{hyp}}$ Opp = $\sqrt{85}$ Hyp = 11 F	Marking NotesScale 15D (0, 5, 9, 12, 15)Consider the solution as requiring four steps:Step 1: Diagram with F, 6, and 11 marked correctlyStep 1: Diagram with F, 6, and 11 marked correctlyStep 2: Pythagoras Theorem fully subbedStep 3: Length of opposite side foundStep 4: Value of sin F found	
	$Hyp^{2} = 0pp^{2} + Adj^{2}$ $(11)^{2} = x^{2} + (6)^{2}$ $x^{2} = 121 - 36 = 85$ $x = \sqrt{85}$ $\sin F = \frac{\sqrt{85}}{11}$	 of 3rd side must have been worked out. Low Partial Credit Work of merit, for example: adj or hyp correctly identified (including on diagram); correct relevant formula One step correct Mid Partial Credit Two steps correct sin 57° = 0 · 838 with or without diagram Uses 6 and 11 as opp and adj and finishes correctly High Partial Credit Three steps correct One error and continues correctly Correct answer without work Full Credit-1 Apply a * if answer is not given in surd form (0 · 838) 	

Q12	Model Solution – 30 Marks	Marking Notes	
(a)	axial symmetry in the line AD	Scale 5B (0, 3, 5)	
		Partial CreditMentions AD	
		Mirror image	
		Axis of symmetry	
		 Full Credit – 1 Apply a * for axial symmetry / line symmetry / reflection in a line, but axis not specified 	

Q12	Model Solution – 30 Marks	Marking Notes	
Q12 (b)	Model Solution – 30 Marks $\sin 60 = \frac{10}{ AB }$ $ AB = \frac{10}{\sin 60}$ $ AB = \frac{20}{2} \text{ [cm] or } \frac{20\sqrt{3}}{2} \text{ [cm]}$	Marking Notes Scale 5C (0, 2, 3, 5) Accept correct answer without units. If calculator is in incorrect mode (radians or gradients), award at most HPC.	
	$ AB = \frac{20}{\sin 60}$ $ AB = \frac{20}{\sqrt{3}} [\text{cm}] \text{ or } \frac{20\sqrt{3}}{3} [\text{cm}]$ OR $\frac{AB}{\sqrt{3}} = \frac{20}{\sqrt{3}} [\text{cm}] \text{ or } \frac{x}{3} = \frac{2}{\sqrt{3}}$ $x = \frac{2\times10}{\sqrt{3}} = \frac{20}{\sqrt{3}} [\text{cm}] \text{ or } \frac{20\sqrt{3}}{3} [\text{cm}]$ OR $\frac{2y}{\sqrt{3}} = \frac{20}{\sqrt{3}} [\text{cm}] \text{ or } \frac{20\sqrt{3}}{3} [\text{cm}]$ OR $(2y)^{2} = (y)^{2} + (10)^{2}$ $4y^{2} = y^{2} + 100$	(radians or gradients), award at most <i>HPC</i> . <i>Low Partial Credit</i> • Some work of merit, for example: relevant drawing with some correct labelling; a correct trigonometric ratio; Pythagoras Theorem • Incorrect trigonometric ratio with AB in numerator, for example tan $60 = \frac{ AB }{10}$, and finishes correctly <i>High Partial Credit</i> • $\sin 60 = \frac{10}{ AB }$ or equivalent (for example, $\frac{x}{2} = \frac{10}{\sqrt{3}}$, $y = \frac{10}{\sqrt{3}}$) • Pythagoras Theorem fully subbed correctly (including $2y$ or $\frac{x}{2}$) • Incorrect trigonometric ratio with AB in denominator, for example tan $60 = \frac{10}{ AB }$, and finishes correctly • Square(s) mishandled in Pythagoras Theorem, otherwise correct • Correct answer without work <i>Full Credit -1</i> • Apply a * if answer is not given in surd form (11 · 54)	
	$3y^{2} = 100$ $y^{2} = \frac{100}{3}$ $y = \frac{10}{\sqrt{3}}$ so $2y = \frac{20}{\sqrt{3}}$ [cm] or $\frac{20\sqrt{3}}{3}$ [cm]		

Q12	Model Solution – 30 Marks		Marking Notes	
Q12 (c)	Model Solution Construction 1: Construction 2: Construction 3: See diagram belo	- 30 Marks Perpendicular bisector of [BC], extended at least to A Bisector of angle at B or C Circle k	Marking NotesScale 20D (0, 5, 10, 15, 20)Tolerance: AD ± 2 mm, angle bisector ± 2°, circle within 2 mm of at least one point of contact.Accept bisector of angle at A for Construction 1, as long as it is extended at least to D.Low Partial Credit• Work of merit in one construction, for example: a relevant construction arc drawnMid Partial Credit• Work of merit in construction 1 and	
			 construction 2 Construction 1 or 2 correct Drawing completed within tolerance but with both Construction 1 and Construction 2 missing construction lines 	
			 High Partial Creat Construction 1 and 2 correct Drawing completed within tolerance but with Construction 1 or Construction 2 missing construction lines or with Construction 1 not fully extended between A and D 	



Q13	Model Solution – 15 Marks	Marking Notes
(a)	S.A. $= 4\pi (9)^2$ = $324\pi \ [m^2]$	Scale 5B (0, 3, 5)Accept correct answer without work.Accept correct answer without units.Partial Credit• Correct formula• Calculates volume of a sphere correctly (i.e. 972π [m³])• $k\pi r^2$ correctly calculated (for $k \neq 4$)Full Credit -1• Apply a * if π omitted (i.e. 324 [m²])• Apply a * if answer is not given in terms of π
(b)	Check extreme values, $r = 8$ and $r = 10$. r = 8: S.A. $= 4\pi(8)^2 = 256\pi$ Error $= 324\pi - 256\pi = 68\pi$ % error $= \frac{68\pi}{256\pi} \times 100 = 26 \cdot 5 \dots = 27\%$ [nearest percent] r = 10: S.A. $= 4\pi(10)^2 = 400\pi$ Error $= 400\pi - 324\pi = 76\pi$ % error $= \frac{76\pi}{400\pi} \times 100 = 19\%$ Max value $= 27\%$	Scale 10D (0, 2, 6, 8, 10) If candidate was awarded <i>Partial Credit</i> in (a) for finding the volume of a sphere, do not penalise candidate in (b) for using volume rather than surface area (max = $42 \cdot 3 \dots = 42\%$ [nearest %]). <i>Low Partial Credit</i> • Work of merit, for example: correct relevant formula; states error = 1 m <i>Mid Partial Credit</i> • Finds surface area when $r = 8$ or $r = 10$ <i>High Partial Credit</i> • Finds surface area when $r = 8$ and $r = 10$ Finds % error when $r = 8$ or $r = 10$ including if estimate from (a) used as denominator <i>Full Credit -1</i> • Apply a * if both percentage errors found but max value not identified

Q14	Model Solution – 5 Marks	Marking Notes	
	$\frac{2}{-\pi R^2 - \pi r^2}$	Scale 5D (0, 2, 3, 4, 5)	
	6	Accept correct answer without units	
	1_{-2} (9) ²	Consider solution as requiring four steps:	
	$\overline{3}R^2 = \left(\overline{2}\right)$	Step 1: $\frac{2}{6}\pi R^2$ and $\pi \left(\frac{9}{2}\right)^2$	
	$\frac{1}{R^2} = \frac{81}{R^2}$	Step 2: Sets up equation	
	$3^{n} - 4$	Step 3: Isolates $R^2 (= \frac{243}{4})$,	
	$R^2 = \frac{243}{4}$	or equivalent (for example, isolates <i>R</i> if circumference is being used)	
	$R = \sqrt{\frac{243}{4}} = \sqrt{\frac{3^5}{4}}$	Step 4: Finds <i>R</i> in required form	
		Note: if circumference used instead of area,	
	then candidate can be considered to have		
	$R = \frac{3^{\frac{3}{2}}}{2}$ [inches]	at most steps 2 and 5 correct.	
	2	Low Partial Credit:	
		• Work of merit, for example:	
		finds radius of small pizza; correct formula	
		Mid Partial Credit	
		• 2 steps correct	
		High Partial Credit	
		• 3 steps correct (including correct answer	
		In incorrect form, for example: $9\sqrt{3}$	
		$/ \cdot /9 \dots \text{ or } \frac{1}{2}$	

Marcanna Breise as ucht freagairt trí Ghaeilge

Léiríonn an tábla thíos an méid marcanna breise ba chóir a bhronnadh ar iarrthóirí a ghnóthaíonn níos mó ná 75% d'iomlán na marcanna.

N.B. Ba chóir marcanna de réir an ghnáthráta a bhronnadh ar iarrthóirí nach ngnóthaíonn níos mó ná 75% d'iomlán na marcanna don scrúdú. Ba chóir freisin an marc bónais sin **a shlánú síos**.

Tábla 300 @ 5%

Bain úsáid as an tábla seo i gcás na n-ábhar a bhfuil 300 marc san iomlán ag gabháil leo agus inarb é 5% gnáthráta an bhónais.

Bain úsáid as an ngnáthráta i gcás 225 marc agus faoina bhun sin. Os cionn an mharc sin, féach an tábla thíos.

Bunmharc	Marc Bónais	Bunmharc	Marc Bónais
226	11	261 - 266	5
227 - 233	10	267 - 273	4
234 - 240	9	274 - 280	3
241 - 246	8	281 - 286	2
247 - 253	7	287 - 293	1
254 - 260	6	294 - 300	0